

**Scheme**  
doc. version 1.1

<b>Arithmetic expressions</b>	
<b>Written version</b>	<b>Scheme version</b>
$5+6+7$	<code>(+ 5 6 7)</code>
$5(6+7)$	<code>(* 5 (+ 6 7))</code>
$\frac{3}{4}$	<code>(/ 3 4)</code> or <code>3/4</code>
$ -4 $ (absolute value)	<code>(abs -4) -&gt; 4</code>
$\sqrt{2}$	<code>(sqrt 2) -&gt; 1.4142135623730951</code>
$\sqrt{-1} = 0 + 1i$	<code>(sqrt -1) -&gt; 0+1i</code>
$2^3$	<code>(expt 2 3) -&gt; 8</code>
$4.87^2$	<code>(sqr 4.87) -&gt; 23.7169</code>
Remainder when 15 is divided by 6 Also written: $15 \bmod 6$	<code>(remainder 15 6) -&gt; 3</code>
$15/6$ after removing the remainder Also written: $\left\lfloor \frac{15}{6} \right\rfloor$	<code>(quotient 15 6) -&gt; 2</code>

<b>Defining variables and functions</b>	
<b>Mathematical version</b>	<b>Scheme version</b>
$a = 5.6$	<code>(define a 5.6)</code>
$b = 2a+3$	<code>(define b (+ (* 2 a) 3))</code>
$f(x) = x+1$	<code>(define (f x) (+ x 1))</code> or <code>(define f (lambda (x) (+ x 1)))</code>
$f(5) \rightarrow 6$	<code>(f 5) -&gt; 6</code>
$g(x,y) = 2x + y$	<code>(define (g fred harry) (+ (* 2 fred) harry))</code>
$h(x,y) = (2x + y)^2$	<code>(define (h a ron) (sqr (+ (* 2 a) ron)))</code> or we can use the function g above (if we've previously defined it)... <code>(define (h a ron) (sqr (g a ron)))</code>
$h(2,3) \rightarrow 49$	<code>(h 2 3) -&gt; 49</code>

<b>Boolean datatype</b>	<b>Scheme written version</b>
TRUE	#t or true
FALSE	#f or false

<b>Comparison operators for numbers</b>	<b>Scheme version</b>
> (greater than)	(> 5 4) -> #t
>= (greater than or equal to)	(>= 5 6) -> #f
= (equal to) (but only for numbers)	(= 5 5.0) -> #t (in WeScheme)
< (less than)	(< 7 6) -> #f
<= (less than or equal to)	(<= 6 6) -> #t

<b>Comparison operator for all simple datatypes (including numbers)</b>	<b>Scheme version</b>
Equal	(equal? 4 4.0) -> #t (in WeScheme) (equal? 4 4.0) -> #f (in SchemingBat) (equal? 4 4.0) -> #f (in DrRacket)  (equal? #t #f) -> #f

<b>Logical conjunction operators</b>	<b>Scheme version</b>
AND	(and #t #t) -> #t (and #f #t) -> #f (and (= 4 4) (> 4 5)) -> #f (and #t #t #f #t #t) -> #f
OR	(or #f #t) -> #t (or #f #f) -> #f (or (= 4 4) (> 4 5)) -> #t (or #f #t #f) -> #t
NOT	(not (= 4 4)) -> #f (correction)

## Decisions using "if"

The IF expression is a list with 4 parts:

**(if test-part true-part false-part)**

The **test-part** is an expression that must return #t or #f. For instance, these three are valid tests:

(> 4 3)

(<= x 0)

(= x (+ 1 y))

Or more complicated ones:

(and (>= x 5) (<= x 10)) ; is x between 5 and 10?

(or (< x 5) (> x 10)) ; is x not between 5 and 10?

In fact, any expression that asks a yes/no question is a valid test.

The **true-part** is an expression that will be evaluated if the **test-part** is True, and its answer will be what the entire if-expression returns

Likewise, the **false-part** will be an expression that will be used (evaluated) if the **test-part** is False, and that will be the answer.

Examples:

(if (> 4 3) (+ 3 1) 18) -> 4

that's because the **test-part**, (> 4 3), is true and so we evaluate the **true-part** (+ 3 1) and that's our answer

(if (= 5 6) (+ 3 1) 18) -> 18

..because the **test-part**, which is (= 5 6), is false, and so the **false-part**, which is 18 is the answer

<b>Functions making decisions using IF</b>	
abs(x) ; the absolute value	<pre>(define (abs x)   (if (&gt;= x 0) ; test-part       x ; true-part       (* -1 x) ; false-part   ) )</pre>
<p>A function f(x), which is equal to:</p> $f(x) = \begin{cases} x^2 + 1 & \text{if } x \geq 3 \\ x - 2 & \text{if } x < 3 \end{cases}$	<pre>(define (f x)   (if (&gt;= x 3)       (+ (* x x) 1)       (- x 2)   ) )</pre> <p>Or, written on a single line:  <pre>(define (f x) (if (&gt;= x 3) (+ (* x x) 1) (- x 2)))</pre></p>
<p>A function grade(score) which is:</p> $\text{grade}(\text{score}) = \begin{cases} 0 & \text{if } \text{score} < 65 \\ 1 & \text{if } \text{score} \geq 65 \text{ and } < 90 \\ 2 & \text{if } \text{score} \geq 90 \end{cases}$	<pre>(define (grade score)   (if (&lt; score 65)       0       (if (and (&gt;= score 65) (&lt; score 90))           1           2       )   ) )</pre>